COLD. Revisiting Hub Labels on the database for large-scale graphs

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Abstract. Shortest-path computation is a well-studied problem in algorithmic theory. An aspect that has only recently attracted attention is the use of databases in combination with graph algorithms to compute distance queries on large graphs. To this end, we propose a novel, efficient, pure-SQL framework for answering exact distance queries on large-scale graphs, implemented entirely on an open-source database system. Our COLD framework (COmpressed Labels on the Database) may answer multiple distance queries (vertex-to-vertex, one-to-many, kNN, RkNN) not handled by previous methods, rendering it a complete solution for a variety of practical applications in large-scale graphs. Experimental results will show that COLD outperforms previous approaches (including popular graph databases) in terms of query time and efficiency, while requiring significantly less storage space than previous methods.

1 Introduction

Answering distance queries on graphs is one of the most well-studied problems on algorithmic theory, mainly due to its wide range of applications. Although a lot of recent research focused exclusively on transportation networks (cf. [9] for the most recent overview) the emergence of social networks has generated massive unweighted graphs of interconnected entities. On such networks, the distance between two vertices is an indication of the closeness of their entities, i.e., for finding users closely related to each other or extracting information about existing communities within the social media users. Although we may always use a breadth first search (BFS) to calculate the distance between any two vertices on such graphs, that approach cannot facilitate fast-enough queries on main memory or be easily adapted to secondary storage solutions.

Moreover, most of the excellent preprocessing techniques available for road networks cannot be adapted to large-scale graphs, such as social or collaboration networks. So far, the most promising approach for this type of graphs builds on the 2-hop labeling or hub labeling (HL) algorithm [23],[12], in which we store a two-part label L(v) for every vertex v: a forward label $L_f(v)$ and a backward label $L_b(v)$. These labels are then used to very fast answer vertex-to-vertex shortest-path queries. This technique has been adapted successfully to road networks [2, 3, 15, 4] and quite recently has also been extended to undirected, unweighted graphs [5, 14, 25]. The HL method has also been applied for one-to-many, many-to-many and kNN queries in road networks [16, 17] and kNN and RkNN queries in the context of social networks in [21].

Although hub labeling is an extremely efficient shortest-path computation method using main memory, there are very few works that try to replicate those algorithms for secondary storage. HLDB [18] stores the calculated hub labels for continental road networks in a commercial database system and translates the typical HL distance query between two vertices to plain SQL commands. Moreover, it showed how to efficiently answer kNN queries and k-best via points, again by means of SQL queries. Recently, HopDB [25] proposed a customized solution that utilizes secondary storage also during preprocessing. Unfortunately, both methods have their shortcomings. HLDB has only been tested on road networks and consequently small labels sizes (<100). Its speed would seriously degrade for large-scale graphs due to the much larger label size. HopDB answers only vertex-to-vertex queries and is a customized C++ solution that cannot be used with existing database systems and, hence, has limited practical applicability.

This work presents a database framework that may service multiple distance queries on massive large-scale graphs. Our pure-SQL COLD framework (COmpressed Labels on the Database) can answer multiple exact distance queries (point-to-point, kNN) in addition to RkNN and *one-to-many* queries not handled by previous methods, rendering it a complete database solution for a variety of practical massive, large-scale graph problems. Our extensive experimentation will show that COLD outperforms previous solutions, including specialized graph databases, on all aspects (including query performance and memory requirements), while servicing a larger variety of distance queries. In addition, COLD is implemented using a popular, open-source database engine with no third-party extensions and, thus, our results are easily reproducible by anyone.

The outline of the remainder of this work is as follows. Section 2 presents related work. Section 3 describes the novel COLD framework and its implementation details. Experiments establishing the benefits of COLD are provided in Section 4. Finally, Section 5 gives conclusions and directions for future work.

2 Related work

Throughout this work we use undirected, unweighted graphs G(V, E) (where V represents vertices and E arcs). A k-Nearest Neighbor (kNN) query seeks the k-nearest neighbors to an input vertex q. The RkNN query (also referred as the monochromatic RkNN query), given a query point q and a set of objects P, retrieves all the objects that have q as one of their k-nearest neighbors according to a given distance function dist(). In graph networks, dist(s, t) corresponds to the minimum network distance between the two objects. Formally RkNN(q) =

 $\{p \in P : dist(p,q) \leq dist(p,p_k)\}$ where p_k is the k-Nearest Neighbor (kNN) of p. Throughout this work, we assume that objects are located on vertices and we always refer to *snapshot* kNN and RkNN queries on graphs, i.e., objects are not moving. Also, similarly to previous works, the term *object density* D refers to the ratio |P|/|V|, where P is a set of objects in the graph and |V| is the total number of vertices. Although, there is extensive literature focusing on kNN and RkNN queries in Euclidean space, since our work focuses on graphs we will only describe related work focusing on the latter.

Regarding road networks and kNN queries, G-tree [33] is a balanced tree structure, constructed by recursively partitioning the road network into subnetworks. Unfortunately, this method cannot scale for continental road networks, since it requires several hours for its preprocessing. Moreover, it requires a *target* selection phase to index which tree-nodes contain objects (requiring few seconds) and thus, cannot be used for moving objects. Recently, the work of [17] expanded the graph-separators CRP algorithm of [13] to handle kNN queries on road networks. Unfortunately, (i) CRP also requires a target selection phase and thus, cannot be applied to moving objects and (ii) it may only perform well for objects near the query location. Hence, this solution is also not optimal. The latest work for kNN queries on road networks is the SALT framework [22] which may be used to answer multiple distance queries on road networks, including vertexto-vertex (v2v), single source (one-to-all, range, one-to-many) and kNN queries. This work expands the graph-separators GRASP algorithms of [20] and the ALT-SIMD adaptation [19] of the ALT algorithm and offers very fast preprocessing time and excellent query times. For kNN queries, SALT does not require a target selection phase and hence it may be used for either static or moving objects.

For $\mathbf{R}k\mathbf{N}\mathbf{N}$ queries on road networks, the work of [30] uses Network Voronoi cells (i.e., the set of vertices and arcs that are closer to the generator object) to answer RkNN queries. This work has only been tested on a relatively small network (110K arcs) and all precomputed information is stored in a database. Despite the fact that the preprocessing stage for computing the Network Voronoi cells is quite costly, the queries' executions times range from 1.5s for D = 0.05and k = 1, up to 32s for k = 20, rendering this solution impractical for real-time scenarios. Up until recently, the only work dealing with other graph classes (besides road networks) is [32], although it has only been tested on sparse networks, e.g., road networks, grid networks (max degree 10), p2p graphs (avg degree 4) and a very small, sparse co-authorship graph (4K nodes). In this work, the conducted experiments for values of k > 1 refer only to road networks, therefore the scalability of this work for denser graphs and larger values of k is questionable. Recently, Borutta et al. [10] extended this work for time-dependent road networks, but presented results were not very encouraging. The larger road network tested had 50k nodes (queries require more than 1s for k = 1) and for a network of 10k nodes and k = 8, RkNN queries take more than 0.3s (without even adding the $I/O \cos t$). In a nutshell, all existing contributions and methods have not been tested on dense, large-scale graphs, cannot scale for increasing kvalues and their performance highly depends on the object density D.

Our work builds upon the 2-hop labeling or Hub Labeling (HL) algorithm of [23, 12] in which, preprocessing stores at every vertex v a forward $L_f(v)$ and a backward label $L_b(v)$. The forward label $L_f(v)$ is a sequence of pairs (u, dist(v, u)), with $u \in V$. Likewise, the backward label $L_b(v)$ contains pairs (w, dist(w, v)). Vertices u and w are denoted as the hubs of v. The generated labels conform to the cover property, i.e., for any s and t, the set $L_f(s) \cap L_b(t)$ must contain at least one hub that is on the shortest s - t path. For undirected graphs $L_b(v) = L_f(v)$. To find the network distance dist(s,t) between two vertices s and t, a HL query must find the hub $v \in L_f(s) \cap L_b(t)$ that minimizes the sum dist(s, v) + dist(v, t). By sorting the pairs in each label by hub, this takes linear time by employing a coordinated sweep over both labels. The HL technique has been successfully adapted for road networks in [2, 3, 15, 4]. In the case of large-scale graphs, the Pruned Landmark Labeling (PLL) algorithm of [5] produces a minimal labeling for a specified vertex ordering. In this work, vertices are ordered by degree, whereas the work of [14] improves the suggested vertex ordering and the storage of the hub labels for maximum compression. The HL method has also been used for one-to-many, many-to-many and kNN queries on road networks in [16] and [17] respectively. Our latest work [21] proposed Re-Hub, a novel main-memory algorithm that extends the Hub Labeling approach to efficiently handle RkNN queries. The main advantage of the *ReHub* algorithm is the separation between its costlier offline phase, which runs only once for a specific set of objects and a very fast online phase which depends on the query vertex q. Still, even the costlier offline phase hardly needs more than 1s, whereas the online phase requires usually less than 1ms, making ReHub the only RkNN algorithm fast enough for real-time applications and big, large-scale graphs.

Regarding secondary-storage solutions, Jiang et al. [25] propose their HopDB algorithm that suggest an efficient HL index construction when the given graphs and the corresponding index are too big to fit into main memory. The work of [1] introduced the HLDB system, which answers distance and kNN queries in road networks entirely within a database by storing the hub labels in database tables and translating the corresponding HL queries to SQL commands. Throughout this work, we will compare our proposed COLD framework to HLDB, since to the best of our knowledge, it is the only framework that may answer exact distance queries entirely within a database. Moreover, within the COLD framework we also adapt our *ReHub* main-memory algorithm into a database context, so that its online phase may be translated to fast and optimized SQL queries.

3 Contribution

This section presents the COLD (COmpressed Labels on the Database) database framework. COLD can answer multiple distance queries (vertex-to-vertex, kNN, RkNN and *one-to-many*) for large-scale graphs using SQL commands. Since COLD builds on HLDB [1] and ReHub [21], we will follow the notation and running example presented there, for highlighting the necessary concepts and challenges for adapting those previous works, (i) in the context of large-scale

$\sim m \sim$	Vertex	Hub Labels (h,d)
(13) Ų(12)	0	(0,0)
$\mathbf{Y} \mathbf{A} \mathbf{Y}$	1	(0,1), (1,0)
O°	2	(0,1), (2,0)
	3	(0,1), (3,0)
X	4	(0,1), (4,0)
(1)	5	(0,2), (1,1), (5,0)
Ĭ	6	(0,2), (1,1), (6,0)
(0)	7	(0,2), (1,1), (7,0)
	8	(0,2), (2,1), (8,0)
(3) + (2)	9	(0,2), (3,1), (9,0)
$\Psi(4)$	10	(0,2), (4,1), (10,0)
AYA	11	(0,3), (1,2), (5,1), (11,0)
๛๛๏	12	(0,3), (1,2), (6,1), (12,0)
	13	(0,3), (1,2), (7,1), (13,0)

Fig. 1 & Table 1: A sample Graph G and the created hub-labels

graphs for [1] and (ii) within the boundaries of a relational database management system (RDBMS) for [21]. To this end, we chose PostgreSQL [29] for our implementation, given that it is a popular, open-source RDBMS. Although we use some PostgreSQL-specific data-types and SQL extensions, we do not use any third-party extensions but only features included in its standard installation.

3.1 Implementation

The COLD framework assumes that we have a correct hub labeling (HL) framework that generates hub-labels for the undirected, unweighted graphs we wish to query. Although COLD will work with any correct HL algorithm, in this work we use the [6] implementation of the PLL algorithm of [5] to generate the necessary labels. To highlight the results of this process, the labels for the undirected, unweighted graph G of Figure 1 are shown in Table 1. Throughout this work, we will refer to those labels as the *forward labels*. The forward label L(v) for a vertex v is an array of pairs (u, dist(v, u) sorted by hub u. Since our work also focuses on snapshot kNN and RkNN queries, there also some objects $P \in V$ that do not change over time. For our specific running example we assume that $P = \{4, 10, 12\}$ and thus, we highlight the respective entries of Table 1.

Vertex-to-Vertex (v2v) queries. To find the network distance dist(s,t) between two vertices s and t, a HL query must find the hub $v \in L(s) \cap L(t)$ that minimizes the sum dist(s, v) + dist(v, t). For our sample graph G, the minimum distance between e.g., vertices 2 and 7 is d(2,7) = 3, using the hub 0. To translate this HL query into SQL commands, in HLDB [1] forward labels are stored in a database table denoted forward where the labels of vertex v are stored as triples of the form (v, hub, dist(v, hub)) (see Table 2). The table forward has the

Table 2: The *forward* table used in HLDB for the sample graph G

\mathbf{v}	hub	\mathbf{dist}	
2	0	1	
2	2	0	
7	0	2	
7	1	1	
7	7	0	

Table 3: The *forwcold* table used for COLD for the sample graph G

v	hubs	dists		
2	$\{0, 2\}$	$\{1, 0\}$		
7	$\{0, 1, 7\}$	$\{2, 1, 0\}$		

```
Code 1.2: V2v query for COLD
    Code 1.1: V2v query for HLDB
1 SELECT MIN(n1.dist+n2.dist)
                                 1 SELECT MIN(n1.d+n2.d) FROM
2 FROM forward n1, forward n2
                                 2 /* Expand hubs, dists arrays */
3 WHERE n1.v = s
                                 3 (SELECT UNNEST(hubs) AS hub,
4 \text{ AND } n2.v = t
                                 4 UNNEST (dists) AS d
5 AND n1.hub = n2.hub;
                                 _5 FROM forwcold WHERE v = s) n1,
                                 6 (SELECT UNNEST(hubs) AS hub,
                                 7 UNNEST (dists) AS d
                                 _8 FROM forwcold WHERE v = t) n2
                                 9 WHERE n1.hub=n2.hub;
```

combination of (v, hub) as the primary key and is clustered according to those columns, so that "all rows corresponding to the same label are stored together to minimize random accesses to the database" [1]. Then we can find the distances between any two vertices s and t by the SQL query of Code 1.1.

Although the HLDB vertex-to-vertex (v2v) query is very simple, there is one major drawback. For such a query, HLDB has to fetch from secondary storage the subset of |L(s)| + |L(t)| rows with common hubs. Although this is practical for road networks where the forward labels have less than 100 hubs per vertex [3], it cannot scale for large-scale graphs where the forward labels have thousand of hubs per vertex. Moreover, on such graphs the forward DB table and the corresponding primary key index will become too large, which is also an important disadvantage. To this end, we take advantage of the fact that PostgreSQL features an array data type that allows columns of a DB table to be defined as variable-length arrays. Hence, in COLD we store hubs and distances for a vertex (both ordered by hub) as arrays in two separate columns (i.e., hubs and dists) in a single row. The resulting forwcold compressed DB table is shown in Table 3. This approach not only emulates exactly how labels are stored on main-memory for fast v2v queries but also has considerable advantages: (i) The forwcold DB table has exactly |V| rows (ii) The forwcold DB table has the column v as primary key without needing a composite key. This alone facilitates faster queries. Moreover the size of the corresponding index will be much smaller. In fact, our experimentation will show that the primary-key index for forwcold may be $> 4,400 \times$ smaller than the index size of HLDB. (iii) For a v2v

Table 4: Necessary data structures for the sample graph G, $P = \{4, 10, 12\}$ and *one-to-many*, kNN and RkNN queries

	0/	1			
	Backward Labels	kNN Backward	ckward RkNN Backward		kNN Result (k=1)
Hub	(to-many) [16]	Labels $(k=2)$ [1]	Labels $(k=1)$ [21]	Obj.	(Obj., dist) [21]
0	(4,1), (10,2), (12,3)	(4,1), (10,2)	(4,1), (12,3)	4	(10 1)
1	(12,2)	(12,2)	(12,2)	-	(10,1)
4	(4,0), (10,1)	(4,0),(10,1)	(4,0), (10,1)	10	(4.1)
6	(12,1)	(12,1)	(12,1)		(4,1)
10	(10,0)	(10,0)	(10,0)	12	(4.4)
12	(12,0)	(12,0)	(12,0)	· * *	(

query, COLD needs to access exactly two rows, regardless of the sizes of |L(s)|and |L(t)|. This way, we efficiently minimized the secondary-storage utilization, even working inside a database. The resulting SQL query for COLD is shown in Code 1.2. There we exploit the fact that PostgreSQL "guarantees that parallel unnesting" for hubs and distances for each nested query "will be in sync", i.e., each pair (hub, dist) is expanded correctly since for the same v the respective arrays have the same number of elements⁴.

Additional queries overview. For answering more complex (kNN, RkNN and *one-to-many*) distance queries on a HL framework for a set of objects P, we need to build some additional data structures from the forward labels (for undirected graphs). Then to answer the respective query we only need to combine the forward labels L(q) of query vertex q, with the respective data structure explained in the following. Those data structures are summarized in Table 4.

For answering *one-to-many* queries, i.e., calculate distances between a source vertex q and all objects in P, we need to build the backward labels-to-many by basically ordering the forward labels of the objects by hub [16] and then by distance for the same hub. For kNN queries we only need to keep at most the k-best pairs (of smallest distances) per hub from the backward labels-to-many to create the kNN backward labels [1]. In our specific example, the kNN backward labels for k = 2 and hub 0, do not contain the pair (12,3). Finally, for RkNN queries, we must first calculate the kNN Results (i.e., the NN of the object 4 is the object 10 with distance 1) and then we build the RkNN backward labels, based on the observation that "we need to access those pairs from the backward labelsto-many to a specific object, if and only if those distances are equal or smaller than the distance of the kNN of this object" [21]. In our specific example, the RkNN backward labels for k = 1 and hub 0, do not contain the pair (10,2) since the NN of object 10 (the object 4) is within distance 1. Although for our small graph the differences between the individual data structures seem minimal, for larger graphs those differences become very prominent. This was also showcased by the theoretical analysis provided in [21] which showed that backward labelsto-many will have on average $D \cdot |HL|$ pairs, the kNN backward labels have at most $k \cdot |V|$ pairs and the RkNN backward labels have on average $\varepsilon \cdot D \cdot |HL|$

⁴ http://stackoverflow.com/a/23838131

Table 5: The *knntab* table used in HLDB for the sample graph G, k = 2 and $P = \{4, 10, 12\}$

[4,10,12]					
hub	\mathbf{dist}	obj			
0	1	4			
0	2	10			
1	2	12			
		$\begin{array}{c c} \mathbf{hub} & \mathbf{dist} \\ \hline \mathbf{hub} & \mathbf{dist} \\ \hline 0 & 1 \\ \hline 0 & 2 \\ \hline 1 & 2 \\ \hline \cdots & \cdots \end{array}$			

Table 6: The *knntab* table used in COLD for the sample graph G, k = 2 and $P = \{4, 10, 12\}$

ι	[1,10,12]					
ſ	hub	\mathbf{dist}	objs			
ſ	0	1	$\{4\}$			
ĺ	0	2	{10}			
ĺ	1	2	$\{12\}$			
[

pairs where ε may be < 0.01 for specific datasets and experimental settings. Moreover, Efentakis et al. [21] have shown how these additional data structures may be constructed from the forward labels in main-memory, requiring less than few seconds, even for the larger tested datasets.

kNN queries. To translate the HL kNN query into SQL, HLDB stores kNN backward labels in a separate DB table denoted knntab that stores triples of the form (hub, dist, obj) (see Table 5). The respective table knntab has the combination of (hub, dist, obj) as a composite primary key and is clustered according to those columns. Note that in HLDB, we cannot use the combination of (hub, dist) as a primary key, because especially in large scale graphs we will have a lot of distance ties even for k-entries for the same hub. Then we can can answer a kNN query from vertex q by the SQL query of Code 1.3. Again, the kNN HLDB query has the same drawbacks as before, i.e., it has to retrieve |L(q)| rows from forward and $k \cdot |L(q)|$ rows from knntab tables, for a total of $(k+1) \cdot |L(q)|$ rows retrieved from secondary storage. Moreover in a database, it makes sense to create one large knntab table for the maximum value kmax of k (e.g., for k = 16) that may be serviced by the DB framework and that same table will be used for all kNN queries up to k = kmax. In that case, the HLDB framework will have to retrieve $(kmax + 1) \cdot |L(q)|$ rows for every kNN query regardless of the value of k.

To remedy the HLDB drawbacks, COLD creates the *knncold* DB table (Table 6) that has the columns (*hub*, *dist*, *objs*), whereas objects are grouped and ordered per hub and distance (the column *objs* is an array). Although for our sample graph G, the DB tables *knntab* and *knncold* seem identical, COLD's method offers several advantages: (i) We can now use the combination of (*hub*, *dist*) as a primary key, which makes the respective index significantly smaller and faster and (ii) In case of many distance ties (common to large-scale graphs) and one large *knncold* DB table that services all *kNN* queries for values of *k* up to the maximum value *kmax*, we only need to fetch the first *k*-objs entries (i.e., objs[1:k]) per hub and dist, which makes the later sorting faster (see Code 1.4).

One-to-many queries. Similar to how COLD handles kNN queries, for oneto-many queries, COLD stores the *backward labels-to-many* in a new *objcold* DB table that has an identical format to *knncold*, i.e., it has three columns (*hub*, *dist*, *objs*) whereas objects are grouped and ordered per hub and distance. Objcold also uses the combination of (*hub*, *dist*) as a primary key. The resulting

```
Code 1.3: kNN query for HLDB
                                       Code 1.4: kNN query for COLD
1 SELECT MIN(n1.dist+n2.dist),
                                   1 SELECT MIN(n1.d+n2.dist).
2 n2.obj FROM
                                   2 UNNEST(objs) AS obj FROM
                                   3 (SELECT UNNEST(hubs) AS hub,
3 forward n1, knntab n2
4 \text{ WHERE } n1.v = q
                                   4 UNNEST(dists) AS d
5 AND n1.hub = n2.hub
                                   _5 FROM forwcold WHERE v = q) n1,
6 GROUP BY n2.obj
                                   6 /* k-entries per hub, dist */
7 ORDER BY MIN(n1.dist+n2.dist)
                                   7 (SELECT hub, dist,objs[1:k]
8 LIMIT k:
                                   8 FROM knncold) n2
                                   9 WHERE n1.hub=n2.hub
                                   10 GROUP BY obj
                                   11 ORDER BY MIN(n1.d+n2.dist)
                                   12 LIMIT k;
```

one-to-many query (Code 1.5) is quite similar to COLD's kNN query, but (i) it operates on the larger objcold DB table (ii) It does not have the ORDER BY ... LIMIT k clause and (iii) We use the entire objs array per hub and distance instead of objs[1:k]. Note that HLDB cannot possibly support such queries because it will need to retrieve on average |L(q)| rows from the forward table and a total of $|L(q)| \cdot D \cdot (|HL|/|V|)$ [21] rows from the corresponding objlab table, which will be prohibitively slow for very large datasets.

Table 7: The *knnres* table used in COLD for R*k*NN queries, the sample graph G, k = 1 and $P = \{4, 10, 12\}$

obj	\mathbf{dists}	objs
4	$\{1\}$	$\{10\}$
10	$\{1\}$	$\{4\}$
12	$\{4\}$	$\{4\}$

Rk**NN queries.** For RkNN queries, COLD stores the RkNN backward labels in a separate *revcold* DB table that has an identical format to previous knncold and *objcold* DB tables, i.e., three columns (*hub*, *dist*, *objs*) where objects are grouped and ordered per hub and distance and the combination of (*hub*, *dist*) used as a primary key. COLD also stores the kNN Results, i.e., the kNN of all ob-

jects in another knnres DB table that has the format (obj, dists, objs,) where obj is the primary key and objs and dists are arrays (both ordered by distance). Therefore the kNN of object p is the objs[k] within distance dists[k] of the respective row for p. Again it makes sense to build a knnres DB table for a max value of kmax that may service RkNN queries for varying values of k. As a result, during the RkNN COLD query, we will have to use an additional JOIN between the revcold and knnres DB tables. The resulting query is shown in Code 1.6.

We see that even the more complex RkNN query in COLD requires just a few lines of SQL code that will work on any recent PostgreSQL version without any need of third-party extensions or specialized index structures. In fact, all DB tables in COLD, use only standard B-tree primary key indexes, without any modifications. To satisfy this strict requirement, we effectively compressed

```
Code 1.5: One-to-many COLD guery
                                      Code 1.6: \mathbf{R}k\mathbf{NN} query for COLD
1 SELECT MIN(n1.d+n2.dist).
                                 1 SELECT n3.id2.n3.dist FROM
2 UNNEST (objs) AS obj FROM
                                  _2 /* n3 subquery is a modified
3 (SELECT UNNEST(hubs) AS hub, 3 one-many-query to revcold */
4 UNNEST (dists) AS d
                                  4 (SELECT MIN(n1.d+n2.dist) AS d3,
5 FROM forwcold
                                  5 UNNEST (objs) AS obj FROM
_{6} WHERE v = q) n1,
                                  6 (SELECT UNNEST (hubs) AS hub,
7 objcold n2
                                  7 UNNEST (dists) AS d
8 WHERE n1.hub=n2.hub
                                  * FROM forwcold WHERE v = q) n1,
9 GROUP BY obj;
                                  9 revcold n2
                                 10 WHERE n1.hub=n2.hub
                                 11 GROUP BY obj
                                 12 ORDER BY obj, MIN(n1.d+n2.dist)
                                 13) n3,
                                 _{14} /* Join with knnres table */
                                 15 (SELECT obj, dists[k] AS dist
                                 16 FROM knnres) n4
                                 17 WHERE n3.obj=n4.obj
                                 18 AND n3.d3<=n4.dist
                                 19 ORDER BY n3.obj;
```

the index sizes by grouping rows per vertex (*forcold* table) or object (*knnres* table), or by hub and distance for *knncold*, *objcold* and *rknncold*. And although we used PostgreSQL specific SQL extensions for expanding the stored arrays, latest versions of other databases (e.g., Oracle) support similar array data-types. Hence, it would be quite easy to port COLD to other database vendors as well.

This section detailed the COLD framework in terms of design and implementation. COLD can answer multiple distance queries (v2v, kNN, RkNN and one-to-many) based on data stored in an off-the-shelf relational database. We also presented the actual queries used and the way the necessary data structures are stored within the database, so that our results are easily reproducible. Although we focused on query efficiency, it is important to note that once we create the *forcold* table, all the adjoining DB tables within COLD may also be created using SQL commands (resulting queries were omitted due to space restrictions). This fact also shows that COLD is truly a pure-SQL framework for servicing multiple distance queries on large-scale graphs. We also provided the necessary theoretical details as to why the COLD framework will outperform existing solutions. This will be further quantified in the following section.

4 Experimental Evaluation

To assess the performance of COLD on various large-scale graphs, we conducted experiments on a workstation with a 4-core Intel i7-4771 processor clocked at 3.5GHz and 32Gb of RAM, running Ubuntu 14.04. We compare our COLD

Table 8: Networks graphs statistics

Graph			Avg degr.	HL / V	PLL Preproc. Time (s)
Facebook	4,039	88,234	22	26	0.03
NotreDame	325,729	1,090,108	3	55	6
Gowalla	196,591	950,327	5	100	13
Youtube	1,134,890	2,987,624	3	167	123
Slashdot1	77,360	469,180	6	204	11
Slashdot2	82,168	504,230	6	216	13
Citeseer1	268,495	1,156,647	4	408	110
Amazon	334,863	925,872	3	689	230
DBLP	540,486	15,245,729	28	3,628	5,720
Citeseer2	434,102	16,036,720	37	4,457	5,946

framework with a custom implementation of HLDB in PostgreSQL and with Neo4j, a well-known, popular graph database.

We use the same network graphs as our previous work of [21] that are taken from the Stanford Large Network Dataset Collection [26] and the 10th Dimacs Implementation Challenge website [8]. All graphs are undirected, unweighted and strongly connected. We used collaboration graphs (DBLP, Citeseer1, Citeseer2) [24], social networks (Facebook [28], Slashdot1 and Slashdot2 [27]), networks with ground-truth communities (Amazon, Youtube) [31], web graphs (Notre Dame) [7] and location-based social networks (Gowalla) [11]. The graphs' average degree is between 3 and 37 and the PLL algorithm creates 26 - 4, 457 labels per vertex, requiring 0.03 - 5, 946s for the hub labels' construction (see Table 8).

COLD and HLDB were implemented in PostgeSQL 9.3.6, 64bit with reasonable settings (8192Mb shared buffers, 64Mb temp buffers). We also used Neo4j Server v2.1.5. The Neo4j queries were formulated using Cypher, Neo4j's declarative query language and we report query times as they were returned by the server. Although Cypher may theoretically facilitate one-to-many queries (besides vertex-to-vertex), testing Neo4j with our datasets and the same number of target vertices we tested COLD with, resulted in a "java.lang.Stack OverflowError". Providing the server with additional resources⁵ had no positive effect and thus there are no results for one-to-many queries and Neo4j.

We conducted experiments belonging to four query types: (i) *vertex-to-vertex*, (ii) kNN, (iii) RkNN and (iv) *one-to-many*. For each experiment, we used 10,000 random start vertices, reporting the average running time. Before each experiment, we restart the PostgreSQL and Neo4j servers for clearing their internal cache and we also clear the operating system's cache for accurate benchmarking. All charts are plotted in logarithmic scale.

4.1 Performance on HDD

In our first round of experiments, we ran experiments on an HDD, specifically a SATA3 Seagate Barracude ST3000DM001 7200*rpm* with 64Mb cache.

⁵ http://neo4j.com/developer/guide-performance-tuning/



Fig. 2: Experiments on HDD for vertex-to-vertex

Vertex-to-vertex. Figure 2(a) shows results for vertex-to-vertex (v2v) queries for COLD, HLDB and Neo4j. Results show that COLD is consistently $2 - 20.7 \times$ faster than HLDB, with this difference amplified for the Citeseer1, Amazon and Youtube datasets (16.8, 19.1 and 20.7 respectively). Moreover, COLD is also $9 - 143 \times$ (for the *Gowalla* dataset) faster than Neo4j, which exhibits stable performance for all datasets, but is slower from both COLD and HLDB. For all datasets, COLD requires less than 9ms for answering v2v queries.

Figure 2(b) shows the difference in memory size for the DB tables forcold (COLD) and forward (HLDB) and their respective primary-key (PK) indexes. Results show that the size of the PK index in COLD is 3,600 - 4,444× smaller than for HLDB (for DBLP and Citeseer2 respectively). As expected, the difference in index sizes is almost identical to the |HL|/|V| ratio, since forcold table has |V| rows and forward has |HL| rows. Likewise, the corresponding tables are 131 - 188× smaller for COLD. Thus, the techniques used for compressing the forward labels in COLD clearly achieve a considerable reduction in memory size, rendering our proposed framework suitable for real-world scenarios.

kNN. Figure 3(a) shows the speedup of COLD compared to HLDB in the case of kNN queries for D = 0.01 and $k = \{1, 2, 4, 8, 16\}$. As described in Section 3.1, we have created two DB tables for each framework (COLD, HLDB), one for kmax = 4 and one for kmax = 16. Then the DB table for kmax = 4 is used for answering kNN queries for k = 1, k = 2 and k = 4 and the kNN table for kmax = 16 is used for answering kNN queries for k = 1, k = 2 and k = 4 and the kNN table for kmax = 16 is used for answering kNN queries for k = 8 and k = 16. Results show that for k = 1, COLD is 5 - 19× faster for the five largest datasets (Amazon, Citeseer, Citeseer2, DBLP. Youtube) and although this speedup degrades for larger values of k, COLD remains consistently 2 - 10× faster even for k = 16. For the smaller datasets, performance between COLD and HLDB is quite similar, with COLD performing better on Facebook and Gowalla, while HLDB performs only marginally better for Slashdot1, Slashdot2 and Notredame. In all cases, COLD answers kNN queries for all datasets in less than 26ms even for k = 16.

In our second set of kNN experiments, we assess the performance of COLD vs HLDB for varying values of D. For each value for D, we have build separate



(a) kNN Speedup of COLD vs (b) Speedup of COLD vs HLDB HLDB for D = 0.01 and varying for k = 4 and varying values of D values of k

Fig. 3: kNN Experiments on HDD for COLD and HLDB

versions of knntab (HLDB) and knncold (COLD) DB tables for $D \cdot |V|$ objects selected at random from each dataset and kmax = 4. Figure 3(b) shows results for k = 4 and $D = \{0.001, 0.005, 0.01, 0.05, 0.1\}$. Again, for the five largest datasets COLD is consistently $3.4 - 23.4 \times$ faster than HLDB, whereas even for the smaller datasets, COLD is consistently $8.6 - 11.5 \times$ faster than HLDB for the largest value of D (for D = 0.1). Moreover, COLD may answer kNN queries for k = 4 on all datasets and all values of D in less than 14ms.

R*k***NN.** For R*k*NN experiments, we only report COLD's performance, since there is no other SQL framework that supports these queries. In out first experiment, we report the performance of COLD for D = 0.01 and $k = \{1, 2, 4, 8, 16\}$. For all those queries we have built one version of the *knnres* DB table for kmax = 16 (see Section 3.1) and 3 separate *revcold* tables for $kmax = \{1, 4, 16\}$. As expected, for RkNN queries and k = 1 we use the *revcold* table built for kmax = 4 and for k = 8, k = 16 we use the *revcold* table built for kmax = 4 and for k = 8, k = 16 we use the *revcold* table built for kmax = 16. Figure 4(a) presents the results. In all cases, COLD provides excellent query times that are below 20ms for k = 1 in all datasets and never exceed 82ms even for k = 16.

In our second set of RkNN experiments, we assess the performance of COLD for varying values of D. Figure 4(b) presents results for k = 1 (as this is the typical case for RkNN queries) and $D = \{0.001, 0.005, 0.01, 0.05, 0.1\}$. Results show that although COLD's performance degrades for larger values of D, RkNN query times are below 49ms for all datasets and values of D, with the exception of Youtube and D = 0.1 (109.3ms). Thus, COLD offers excellent and stable performance in RkNN queries for all all datasets and tested values of k and D.

One-to-Many. Again, COLD is the only SQL framework that supports *one-to-many queries*. Figure 5(a) presents the corresponding results for varying values of D ($D = \{0.001, 0.005, 0.01, 0.05, 0.1\}$). COLD answers such queries in less than a



(a) One-to-Many experiments for (b) CC COLD varying values of D SSD

(b) COLD One-to-Many HDD vs SSD

Fig. 5: One-to-many experiments for COLD

second for all datasets and values of D, except the Citeseer2 and DBLP datasets (those with the highest |HL|/|V| ratio) that require 5601ms and 4170ms respectively, for D = 0.1. For such high values of D, the one-to-many query reaches the complexity of an one-to-all query and as expected, it cannot be any faster on a secondary storage device. Note that even specialized graph databases like Neo4j cannot support this type of queries for more than a 1,000 target objects, whereas COLD answers one-to-many queries to 110,000 target objects in the Youtube dataset in 401ms with a simple SQL query.

4.2 Performance on SSD

Having established the performance characteristics of COLD in the HDD, in our second round of experiments, we repeat some of the previous experiments, using a SSD to measure the impact of the secondary-storage device type to results. The SSD used is a SATA3 Crucial CT512MX100SSD1 MX100 512GB 2.5".



Fig. 7: kNN and RkNN SSD performance



Fig. 6: SSD vertex-to-vertex

Vertex-to-vertex. Although the usage of SSD favors HLDB more than COLD (see Figure 6), COLD is consistently 1.6 - $3.2 \times$ faster than HLDB (except Facebook, the smallest of datasets). The SSD has almost no impact on Neo4j and thus, COLD is now $11-171 \times$ faster than Neo4j on all datasets. Note, than on the SSD, COLD requires less than 0.9ms for all datasets and v2v queries, except the Citeseer2 and DBLP datasets (those with the highest |HL|/|V| ratio). But even then, vertex-to-vertex queries still re-

quire less than 2.6ms for COLD.

kNN. Figure 7(a) shows the performance speedup of COLD compared to HLDB in the case of kNN queries running on the SSD, for D = 0.01 and varying value of k. Again, although the SSD lowers the performance gap between COLD and HLDB, COLD is still faster on all datasets (except Facebook). In fact, COLD is 2.6 - 6.75× faster than HLDB for the high |HL|/|V| ratio datasets (Citeseer2, HLDB) requiring less than 24.6ms even for k = 16.

Rk**NN**. Figure 7(b) presents the results of the RkNN query time performance on COLD for D = 0.01 and varying value of k. Results show that SSD usage accelerates COLD by only 20% at most, which clearly demonstrates that COLD effectively minimized secondary storage utilization and thus adding a better secondary-storage medium provides minimal benefits for RkNN queries.

One-to-Many. Finally, Figure 5(b) compares *one-to-many* queries on HDD and SSD for COLD. Again, the SSD usage accelerates COLD by only 2- 30%, which further confirms the optimal secondary storage utilization of COLD.

4.3 Summary

Our experimentation has shown that our proposed COLD framework outperforms previous state-of-the-art HLDB in all performance benchmarks, including query performance, memory size and scalability. Using HDDs, COLD is $2-21 \times$ faster for *vertex-to-vertex* queries and $5-19 \times$ faster for kNN queries and the largest datasets. Using SSDs, COLD is $1.6 - 3.2 \times$ faster than HLDB for *vertexto-vertex* and up to $6.75 \times$ faster for kNN queries. COLD also requires up to $4,444 \times$ less storage space (indexes) and up to $188 \times$ less storage space (DB tables) used for storing forward labels. Even specialized graph databases like Neo4j are outperformed by COLD, which is up to $143 \times$ faster. Most importantly COLD may service additional (RkNN, one-to-many) queries, not handled by any other previous secondary-storage solutions, while providing excellent query times and optimal secondary-storage utilization even on standard hard drives.

5 Conclusions

This work presented COLD, a novel SQL framework for answering various exact distance queries for large-scale graphs on a database. Our results showed that COLD outperforms existing solutions (including specialized graph databases) on all levels, including query performance, secondary storage utilization and scalability. Moreover, COLD also answers RkNN and one-to-many queries, not handled by previous methods. This establishes COLD as a competitive database-driven framework for querying large-scale graphs. The paper gives the design and implementation details of COLD using a popular, open-source database system along with the actual SQL queries used in our implementation. This should allow for a simple replication of our results and encourage other researchers to expand the COLD framework towards handling more complex queries and test-cases.

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